

Prove each identity:

1.  $\sec x - \tan x \sin x = \frac{1}{\sec x}$

$$\frac{1}{\cos} - \frac{\sin \sin}{\cos}$$

$$\frac{\cos^2}{\cos}$$

$$\frac{1}{\cos x} = \frac{1}{\sec x}$$

2.  $\frac{1 + \cos x}{\sin x} = \csc x + \cot x$

$$\frac{1}{\sin x} + \frac{\cos x}{\sin x}$$

$$\csc x + \cot x = \csc x + \cot x$$

3.  $\frac{\sec \theta \sin \theta}{\tan \theta + \cot \theta} = \sin^2 \theta$

$$\frac{1}{\cos} \cdot \sin$$

$$\frac{\sin}{\cos}$$

$$\frac{\frac{\sin}{\cos} + \frac{\cos}{\sin}}{\frac{\sin^2 + \cos^2}{\sin \cos}}$$

$$\frac{\sin x}{\cos x} \cdot \frac{\sin x \cos x}{1} = \sin^2 x = \sin^2 x$$

4.  $\frac{\sec \theta}{\cos \theta} - \frac{\tan \theta}{\cot \theta} = 1$

$$\frac{1}{\cos \theta} = \frac{1}{\cos^2 \theta} - \frac{\sin \cos}{\cos / \sin}$$

$$\frac{1 - \sin^2 \theta}{\cos^2 \theta} = \frac{\cos^2 \theta}{\cos^2 \theta} = 1 = 1$$

5.  $\cos^2 y - \sin^2 y = 1 - 2\sin^2 y$

$$1 - \sin^2 y - \sin^2 y$$

$$1 - 2\sin^2 y = 1 - 2\sin^2 y$$

6.  $\csc^2 \theta \tan^2 \theta - 1 = \tan^2 \theta$

$$\frac{1}{\sin^2 \theta} \cdot \frac{\sin^2}{\cos^2} - 1$$

$$\frac{1}{\cos^2 \theta} - 1$$

$$\sec^2 \theta - 1$$

$$\tan^2 \theta = \tan^2 \theta$$

7.  $\frac{\sec^2 \theta}{\sec^2 \theta - 1} = \csc^2 \theta$

$$\frac{\sec^2 \theta}{\tan^2 \theta} = \frac{1}{\frac{\cos^2 \theta}{\sin^2 \theta}} = \frac{\sin^2 \theta}{\cos^2 \theta}$$

$$\frac{1}{\cos^2 \theta} \cdot \frac{\cos^2 \theta}{\sin^2 \theta} = \frac{1}{\sin^2 \theta} = \csc^2 \theta$$

8.  $\tan^2 x \sin^2 x = \tan^2 x - \sin^2 x$

$$\frac{\sin^2 x}{\cos^2 x} \sin^2 x$$

$$\frac{\sin^2 x}{\cos^2 x} (\sec^2 x - 1) \sin^2 x$$

$$\sec^2 x \sin^2 x - \sin^2 x$$

$$\frac{\sin^2 x}{\cos^2 x} - \sin^2 x$$

$$\tan^2 x - \sin^2 x = \tan^2 x - \sin^2 x$$

$$16) \frac{\sec x + \tan x}{1 + \sec x} = \frac{\sec x + \frac{\sin x}{\cos x}}{1 + \frac{1}{\cos x}} = \frac{\frac{\sec x \cos x + \sin x}{\cos x}}{\frac{\cos x + 1}{\cos x}}$$

$$\frac{\sec x \cos x + \sin x}{\cos x} \cdot \frac{\cos x}{\cos x + 1} = \frac{\sec x (\cancel{\cos x} + 1)}{\cancel{\cos x} + 1} = \sec x = \frac{1}{\cos x}$$

$$15) \frac{\tan \theta}{\sec \theta} + \frac{\cot \theta}{\csc \theta} = \frac{\frac{\sin \theta}{\cos \theta}}{\frac{1}{\cos \theta}} + \frac{\frac{\cos \theta}{\sin \theta}}{\frac{1}{\sin \theta}} = \sin \theta + \cos \theta$$

$$14) \csc^4 x - \cot^4 x = (\csc^2 x + \cot^2 x)(\csc^2 x - \cot^2 x)$$

$$(1 + \cot^2 x + \cot^2 x)(1 + \cot^2 x - \cot^2 x)$$

$$1 + 2\cot^2 x$$

$$1 + \frac{2\cos^2 x}{\sin^2 x}$$

$$\frac{\sin^2 x + 2\cos^2 x}{\sin^2 x}$$

$$\frac{1 - \cos^2 x + 2\cos^2 x}{\sin^2 x}$$

$$\frac{1 + \cos^2 x}{\sin^2 x}$$

$$\frac{1}{\sin^2 x} - \frac{\cos^2 x}{\sin^2 x}$$

$$\csc^2 x - \cot^2 x = \csc^2 x \cot^2 x$$

$$13) \frac{\cos x + 1}{\sin^3 x} = \frac{\cos x}{\sin^3 x} + \frac{1}{\sin^3 x}$$

$$\frac{\cos}{\sin(\sin^2)}$$

$$\frac{1}{\sin(1 - \cos x)}$$

$$\frac{\cot x}{\sin^2 x} + \frac{1}{\sin^3 x} = \frac{\sin \cot + 1}{\sin^3 x}$$

$$\frac{\cos}{\sin} \left( \frac{1}{\sin^2} \right) + \frac{1}{\sin^3}$$

$$\frac{\cot}{\sin^2} + \csc^3 = \frac{\cos}{\sin} \left( \frac{1}{\sin^2} \right) + \frac{1}{\sin^3}$$

$$\frac{\cos}{\sin} \left( \frac{1}{\sin^2} \right) + \frac{1}{\sin^3}$$

$$\frac{\cos \csc^2}{\sin} + \csc^3$$

$$\frac{\cos \csc^2 + \sin \csc^3}{\sin}$$

$$\frac{\csc^2 (\cos + \sin \csc)}{\sin}$$