Simplify each and state the excluded values.

1)
$$\frac{45n-36}{18n+81}$$

$$2) \ \frac{-p^2 + 12p - 27}{p^2 - 10p + 21}$$

Simplify each expression.

$$3) \ \frac{27a^3}{2a^2} \cdot \frac{14a^3 + 16a^2}{63a + 72}$$

4)
$$\frac{k+1}{k^2+5k-50} \cdot \frac{-k^2+9k-20}{k^2-2k-3}$$

5)
$$\frac{3a-3}{a-1} \div \frac{3a+15}{2a+10}$$

6)
$$\frac{n^2 - 5n - 24}{6n + 18} \div \frac{n^2 - 12n + 32}{n^2 - 9n + 20}$$

7)
$$\frac{2b}{3} - \frac{b+2}{2b+14}$$

8)
$$\frac{8m}{7m^2 + 7m} - 8m$$

9)
$$\frac{6}{n-6} + \frac{2}{n+5}$$

10)
$$\frac{5}{v+2} + \frac{4}{5v+4}$$

$$11) \ \frac{\frac{5}{m} + \frac{m}{9}}{3}$$

12)
$$\frac{\frac{a^2}{a+2} - \frac{25}{a+2}}{\frac{1}{a+2} + \frac{5}{3}}$$

Solve each equation. Remember to check for extraneous solutions.

13)
$$\frac{2}{n^2} = \frac{5}{2n} + \frac{1}{n^2}$$

14)
$$\frac{1}{x^2 - 3x - 18} = 1 - \frac{x+1}{x+3}$$