

Solving Rationals HW

Solve each equation. Remember to check for extraneous solutions.

1) $\frac{r-3}{r} + 2 = \frac{r-1}{r}$

$$r-3+2r = r-1$$

$$2r = 2$$

$$r = 1$$

2) $\frac{1}{2} + \frac{1}{4} = \frac{x-1}{2x}$

$x = -2$

3) $\frac{5}{a} = \frac{1}{2a} + 1$

$$10 = 1 + 2a$$

$$\frac{9}{2} = a$$

4) $\frac{1}{4n} = \frac{5}{n} - \frac{3n-12}{4n^2}$

$x = -3/4$

5) $\frac{6}{v} - \frac{1}{2} = \frac{v}{2}$

$$12 - v = v^2$$

$$0 = v^2 + v - 12$$

$$0 = (v+4)(v-3)$$

$$v = -4, 3$$

6) $\frac{1}{2} = \frac{1}{4x^2} + \frac{x^2+4x-5}{4x^2}$

$x = 2$

7) $\frac{1}{r^2} = \frac{r-4}{r^2} - \frac{r^2-1}{r^3+4r^2}$

$$1(r+4) = (r-4)(r+4) - [r^2-1]$$

$$r+4 = r^2 - 16 - r^2 + 1$$

$$r = -19$$

8) $1 - \frac{x+6}{2x^2+6x} = \frac{1}{2x+6}$

$x = 1$

9) $\frac{m+6}{3} + \frac{m+2}{3m-3} = \frac{m}{m-1}$ $m = -4$ ~~$m = 1$~~

$$3(m-1)$$

$$(m+6)(m-1) + m+2 = 3m$$

$$m^2 + 5m - 6 + m + 2 = 3m$$

$$m^2 + 3m - 4 = 0$$

$$(m+4)(m-1) = 0$$

10) $1 = \frac{2}{n+3} - \frac{5n-10}{n-5}$

$x = 7/3, -5/2$

Rational Inequalities

Name _____

Date _____

Solve each inequality.

1) $\frac{x+1}{x+7} > 0$

$(-\infty, -7) \cup (-1, \infty)$

2) $\frac{x+5}{x+3} < 0$

$(-5, -3)$

3) $\frac{x-9}{x+6} > -2$

$(-\infty, -6) \cup (-1, \infty)$

4) $\frac{2x-21}{5x-35} \geq -1$

$(-\infty, 7) \cup [8, \infty)$

5) $\frac{x^2-2x-24}{x+5} \leq 0$

$(-\infty, -5) \cup [-4, 6]$

6) $\frac{x^2+11x+28}{x-5} < 0$

$(-\infty, -7) \cup (-4, 5)$

7) $\frac{5x+44}{2x+12} > -1$

$(-\infty, -8) \cup (-6, \infty)$

8) $\frac{-x+3}{x-1} \geq 1$

$(1, 2]$

9) $\frac{x^2-16x+64}{x-2} \geq 0$

$(2, \infty)$

10) $\frac{x+7}{x^2+3x-40} > 0$

$(-8, -7) \cup (5, \infty)$

11) $\frac{15}{x+8} \geq \frac{14}{x+7}$

$(-8, -7) \cup [7, \infty)$

12) $\frac{4}{x} \geq \frac{3}{x+1}$

$[-4, -1) \cup (0, \infty)$

13) $\frac{x-7}{(x+5)(x+7)} \geq 0$

$(-7, -5) \cup [7, \infty)$

14) $\frac{x-6}{(x+2)(x-7)} \leq 0$

$(-\infty, -2) \cup [6, 7)$