

Recursive Sequences

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Recursion: a process in which each step of the pattern is **dependent on the previous term.**

Recursive Formulas

Arithmetic:
 $d =$ Common
 difference

$$a_n = a_{n-1} + d$$

$$a_1 = \underline{\hspace{2cm}}$$

$a_{n-1} =$ Previous
 term

Geometric:
 $r =$ Common
 ratio

$$a_n = r \cdot a^{n-1}$$

$$a_1 = \underline{\hspace{2cm}}$$

$a_2 = (-2) \cdot a_1$
 $= -2(-8) = 16$
 $a_3 = -2 \cdot a_2$
 $= -2(16) = -32$

Find the recursive equation given the following:

1. 2, -5, -12, -19, ... $d = -7$

$$a_n = a_{n-1} + d$$

$$a_1 = \underline{\hspace{2cm}}$$

$$a_n = a_{n-1} - 7$$

$$a_1 = 2$$

2. 100, 50, 25, ... $r = \frac{1}{2}$

$$a_n = r \cdot a^{n-1}$$

$$a_1 = \underline{\hspace{2cm}}$$

$$a_n = (\frac{1}{2}) \cdot a^{n-1}$$

$$a_1 = 100$$

3. $a_n = 5 - 2(n-1)$
 $a_n = a_1 + d(n-1)$
 $a_1 = 5 \quad d = -2$

$$a_n = a_{n-1} - 2$$

$$a_1 = 5$$

4. $a_n = 5(-2)^n$
 $a_1 = 5(-2)^1 = -10$
 $r = -2$

$$a_n = r \cdot a^{n-1}$$

$$a_1 = \underline{\hspace{2cm}}$$

$$a_n = (-2) a^{n-1}$$

$$a_1 = -10$$

Find the first 3 terms of each arithmetic sequence and write the recursive formula:

1. $a_1 = 43$ $d = 10$ $a_n = a_{n-1} + 10$
 $a_1 = 43$

$$a_2 = a_{2-1} + 10$$

$$a_2 = a_1 + 10 = 43 + 10 = 53$$

$$a_3 = a_{3-1} + 10 = 53 + 10 = 63$$

2. $a_1 = -8$ $r = -2$ $a_n = (-2)a_{n-1}$
 $a_1 = -8$

$$a_2 = (-2)a_{2-1}$$
$$= -2(-8) = 16$$

$$a_3 = -2 \cdot a_{3-1}$$

$$-2(16) = -32$$

Find the first ⁽⁴⁾ five terms of the following sequences.

1. $a_1 = 2, a_n = (a_{n-1})^2 + 3$

2. $a_n = 2a_{n-1} + a_{n-2}$

$$a_1 = 3, a_2 = 5$$

3. $a_1 = 2, a_n = (-1)^{n-1} \cdot 3a_{n-1}$

Find the first 3 terms of each arithmetic sequence and write the recursive formula:

1. $a_1 = 43$ $d = 10$

$$a_n = a_{n-1} + 10$$

$$a_1 = 43$$

$$a_2 = a_{2-1} + 10$$

$$a_2 = a_1 + 10$$

$$a_2 = 43 + 10 = \underline{53}$$

$$a_3 = a_{3-1} + 10$$

$$a_3 = a_2 + 10$$

$$= 53 + 10 = \underline{63}$$

2. $a_1 = -8$ $r = -2$

$$a_n = r \cdot a_{n-1}$$

$$a_1 = -8$$

$$a_2 = r \cdot a_{2-1}$$

$$= (-2)(-8) = 16$$

$$a_3 = (-2)(16) = -32$$

Find the first ³ ~~five~~ terms of the following sequences.

1. $a_1 = 2$, $a_n = (a_{n-1})^2 + 3$ $a_2 = 7$ $a_3 = 52$

$$a_2 = (a_{2-1})^2 + 3$$

$$a_2 = (2)^2 + 3 = 7$$

$$a_3 = (a_{3-1})^2 + 3$$

$$= (7)^2 + 3 = 52$$

$$a_4 = (a_3)^2 + 3$$

$$(52)^2 + 3 = 2707$$

2. $a_n = 2a_{n-1} + a_{n-2}$ $a_3 = 13$

$a_1 = 3$, $a_2 = 5$

$$a_3 = 2a_{3-1} + a_{3-2}$$

$$= 2a_2 + a_1$$

$$= 2(5) + 3 = 13$$

$$a_4 = 2a_3 + a_2$$

$$= 2(13) + 5$$

$$= 31$$

3. $a_1 = 2$, $a_n = (-1)^{n-1} \cdot 3a_{n-1}$ $a_2 = (-1)^{2-1} \cdot 3a_{2-1}$

$$= -1 \cdot 3(2) = -6$$

$$a_3 = (-1)^{3-1} \cdot 3a_{3-1}$$

$$1 \cdot 3 \cdot (-6) = -18$$

$$a_4 = (-1)^{4-1} \cdot 3(-18)$$

$$= -1(-54) = 54$$

Given the sequence $a_n = a_{n-1} + 4n$ and $a_5 = 487$, find the first term.

$$a_5 = a_4 + 4(5)$$

$$487 = a_4 + 20$$

$$467 = a_4$$

$$a_4 = a_3 + 4(4)$$

$$467 = a_3 + 16$$

$$451 = a_3$$

$$a_3 = a_2 + 4(3)$$

$$451 = a_2 + 12$$

$$439 = a_2$$

$$a_2 = a_1 + 4(2)$$

$$439 = a_1 + 8$$

$$\boxed{431 = a_1}$$