

Review for Test

Test will cover:

- *Sequences and Series
- *Recursive & Explicit form
- *Sigma Notation
- *Applications
- *Binomial Theorem
- *Limits

Find the next 2 terms in the sequence. Then write a recursive **and** an explicit equation.

1. 4, 9, 14, ...

$$d=5 \left\{ \begin{array}{l} R \left\{ \begin{array}{l} a_n = a_{n-1} + 5 \\ a_1 = 4 \end{array} \right. \\ E \left\{ \begin{array}{l} a_n = 4 + 5(n-1) \\ 4 + 5n - 5 \\ -1 + 5n \end{array} \right. \end{array} \right.$$

2. 1000, 800, 640, ...

$$r=.8 \left\{ \begin{array}{l} E \left\{ a_n = 1000(.8)^{n-1} \right. \\ R \left\{ \begin{array}{l} a_n = a_{n-1}(.8) \\ a_1 = 1000 \end{array} \right. \end{array} \right.$$

Write the explicit equation for the arithmetic sequence given $a_{11} = 80$ and $a_{30} = 251$.

$$a_n = a_1 + d(n-1)$$

$$80 = a_1 + 9(10) \quad a_1 = -10$$

$$251 = a_1 + 19(19) \quad a_1 = -10$$

$$a_n = -10 + 9(n-1) = -10 + 9n - 9 = 9n - 19$$

2. Geometric, $a_2 = -15$ and $a_5 = -1875$

$$a_n = a_1(r)^{n-1}$$

$$-15 = a_1(5)^1 \quad a_1 = -3$$

$$-1875 = -3(5)^{4} \quad r = 5$$

$$a_n = -3(5)^{n-1}$$

Write the following in summation notation. Then find the sum.

1. $-1 + 3 + 7 + 11 + \dots n = 11$

$$\sum_{i=1}^{11} (4n-5)$$

$$S_{11} = \frac{11}{2}(-1+39) = 209$$

$$a_n = -1 + 4(n-1) = -1 + 4n - 4 = 4n - 5$$

2. $2, 6, 18, \dots n = 8$

$$\sum_{i=1}^8 2(3)^{n-1}$$

$$S = \frac{2(1-3^8)}{1-3} = 6560$$

$$a_n = 2(3)^{n-1}$$

Sum geo

Find the number of terms given the following.

1. $a_1 = 18, d = 3, S_n = 363$ $a_n = 18 + 3n - 3 = 15 + 3n$

$$363 = \frac{n}{2}(18 + 15 + 3n)$$

$$726 = 3n^2 + 33n$$

$$n = 11$$

2. $a_1 = 2, r = 4, S_n = 10922$

$$10922 = 2 \frac{(1 - 4^n)}{1 - 4}$$

$$16384 = 4n$$

$$n = 7$$

Find the sum of the series.

1. $\sum_{n=1}^8 243(1/3)^{n-1}$ $S_n = \frac{a_1(1-r^n)}{1-r}$

$$S_8 = \frac{243(1 - \frac{1}{3^8})}{1 - \frac{1}{3}} \approx 364.44 = \frac{3280}{9}$$

2. $\sum_{n=3}^{15} (4n^2 - 3) = \frac{13}{2} (9 + 57) = 429$

Find the sum of the series.

1. $a_n = (-1)^{n-1} \cdot 3a_{n-1}$ for 4 terms given $a_1 = 3$

$$a_2 = (-1)^1 (3)(3) = -9$$

$$a_3 = (-1)^2 (3)(-9) = -27$$

$$a_4 = (-1)^3 (3)(-27) = -81$$

$$= -48$$

2. $\sum_{n=3}^5 (2^{n-1} + 4n) = 76$

$$2^{3-1} + 4(3) = 16$$

$$2^{4-1} + 4(4) = 24$$

$$2^{5-1} + 4(5) = 36$$

Determine if the series converges. If so, find its sum.

1. $\sum_{k=1}^{\infty} 4(3/4)^{k-1}$ **Converges**

$$S = \frac{a_1}{1-r} = \frac{4}{1 - \frac{3}{4}} = 16$$

2. $\frac{1}{8} + \frac{1}{16} + \frac{1}{32} + \dots$ **Converges**

$$\sum_{n=1}^{\infty} \frac{1}{8} \left(\frac{1}{2}\right)^{n-1} = \frac{1/8}{1 - 1/2} = \frac{1}{4}$$

b.)

$$36,000 + 1500(n-1)$$

$$180,000 = 36,000 + 1500n - 1500$$

$$n = 97$$

notebook

is dropped from 25 feet off the ground. The ball bounces .7 high of the previous bounce height.

- Write an explicit equation.
- How tall will the ball be after 6 bounces?
- How many bounces until the ball is less than a foot?
- What is the total height the ball travels?

$a_0 = 25$

$a_1 = 17.5$

$a_n = 17.5(0.7)^{n-1}$

$a_6 = 17.5(0.7)^5 \sim 2.94$

$1 = 17.5(0.7)^{n-1}$ No

$n \sim 9.02$ after 10

$S = \frac{95}{1-0.7} \approx 316.67$

Expand the following.

1. $(3x^2 - 1)^5$

$$1(3x^2)^5(-1)^0 + 5(3x^2)^4(-1)^1 + 10(3x^2)^3(-1)^2 + 10(3x^2)^2(-1)^3 + 5(3x^2)^1(-1)^4 + 1(3x^2)^0(-1)^5$$

2. $(4a^4 + b)^4$

$$1(4a^4)^4(b^0) + 4(4a^4)^3(b)^1 +$$

1.) $243x^{10} - 405x^8 + 270x^6 - 90x^4 + 15x^2 - 1$

1. Find the 3rd term in $(2b - 3)^4$

$$6(2b)^2(-3)^2$$

$$6(4b^2)(9) = 216b^2$$

2. Find the coefficient of y^2 in $(4 - y)^3$

$$1(4)^3 + 3(4)^2(-y) + 3(4)(-y)^2 + 1(-y)^3$$

$\sim 48 \quad \underline{12}$

3. Find the 5th term in $(1 + 4y^3)^4$

$$1(4y^3)^4(1)^0$$

$$256y^{12}$$

Find the following limits.

1) $f(0) = 4$

2) $\lim_{x \rightarrow 0} = 0$

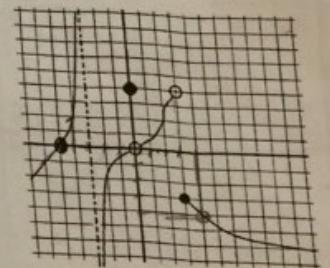
3) $\lim_{x \rightarrow -4} = 2$

4) $\lim_{x \rightarrow 3} = \text{DNE}$

5) $\lim_{x \rightarrow 3} = -\infty$

6) $f(4) = -4$

7) $f(-3) = \text{DNE}$



Find the limits.

$$1) \lim_{x \rightarrow -2} \frac{x^2 - 4}{x + 2} = \frac{(x+2)(x-2)}{x+2} = -4$$

$$2) \lim_{x \rightarrow 4} \frac{\sqrt{x} - 2}{x - 4} \cdot \frac{\sqrt{x} + 2}{\sqrt{x} + 2} = \frac{1}{4}$$

$$3) \lim_{x \rightarrow 3} f(x), f(x) = \begin{cases} 2x - 9, & x \leq 3 \\ -1, & x > 3 \end{cases}$$

$$2(3) - 9 = -3$$

$$4) \lim_{x \rightarrow \infty} \frac{3 - 4x^2}{x^2 + 3x + 2}$$

$$\frac{x^2(\frac{3}{x^2} - 4)}{x^2(1 + \frac{3}{x} + \frac{2}{x^2})} = -4$$

$$5) \lim_{x \rightarrow 3} \frac{x}{\frac{1}{3+x} - \frac{1}{3}} = 0$$

$$6) \lim_{x \rightarrow -1} \left(-\frac{x^2}{2} - 3x + \frac{1}{2} \right) = 3$$

$$-\frac{1}{2} + 3 + \frac{1}{2}$$

$$7) \lim_{x \rightarrow 2} \frac{x-2}{x^3-8} = \frac{1}{12}$$

$$\begin{aligned} 5) \frac{x}{3 - (3+x)} &= \frac{x}{-x} \\ &= \frac{x}{1} \cdot \frac{3(3+x)}{-x} = \frac{(9+3x)}{-1} \\ &= \frac{9+3(-3)}{-1} \\ &= 0 \end{aligned}$$